

LoRaWAN: single gateway capacity for a reasonable traffic

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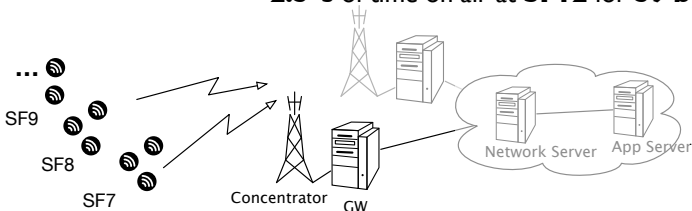
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Capacity of a LoRaWAN cell

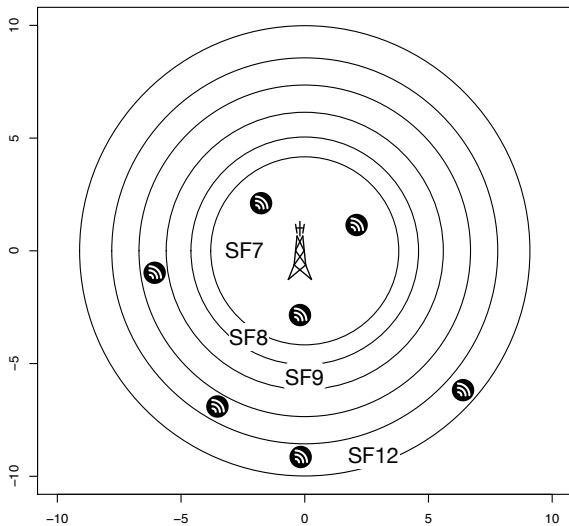
- **How many nodes** can a single GW handle?
 - ✓ We are looking at **uplink capacity** only!
- LoRaWAN transmissions
 - ✓ **Aloha** access
 - ▶ With **physical capture**!
Reception of a given frame if the colliding frame is 6 dB weaker³
 - ✓ Several spreading factors SF7 — SF12
 - ▶ **Quasi-orthogonal** symbols (16 to 36 dB rejection)¹
 - ▶ Transmission duration \sim doubles from SF_n to SF_{n+1}
 - ✓ Stringent **duty cycle** limitations (**1%** in each sub-band)
 - ✓ *Relatively short frames*

2.5 s of time on air at **SF12** for **59 bytes**!



³Dedicated networks for IoT : PHY / MAC state of the art and challenges, C.

SF boundaries



Previous work

Low Power Wide Area Network Analysis: Can LoRa Scale?

O. Georgiou and U. Raza

IEEE Wireless Communications Letters **2017**

signals since the system is assumed ergodic (i.e., any two instances of time are statistically independent). Note that the transmit powers of end-devices with the same SF signals are assumed equal. The second outage condition is therefore given by the complement of:

$$Q_1 = \mathbb{P}\left[\frac{|h_1|^2 g(d_1)}{|h_{k^*}|^2 g(d_{k^*})} \geq 4 \mid d_1\right], \quad (4)$$

thus providing a statistically meaningful performance metric quantifying when collisions of the same SF are significant. Intuitively, we expect Q_1 to decay with increasing \tilde{N} .

Combined, the two outage conditions form the joint outage probability J_1 of a received signal s_1 given by the complement of a successfully received signal defined as $J_1 = 1 - H_1 Q_1$.

3) *Coverage Probability*: The coverage probability is the probability that a randomly selected end-device is in coverage (i.e., not in outage) at any particular instance of time. One may obtain the system's coverage probability \wp_c with respect

given by $f_{d_i}(x) = 2\pi x / |\mathcal{V}(d_1)|$. Calculating the pdf of $g(d_i)$

$$f_{g(d_i)}(x) = \left| \frac{d}{dx} g^{-1}(x) \right| f_{d_i}(g^{-1}(x)) = \frac{\lambda^2 x^{-\frac{\eta+2}{\eta}}}{8\eta\pi |\hat{\mathcal{V}}(d_1)|} \quad (8)$$

which has a finite support on $g(l_{j+1}) \leq x \leq g(l_j)$, and recalling that $|h_i|^2 \sim \exp(1)$, it follows that the pdf of X_i is

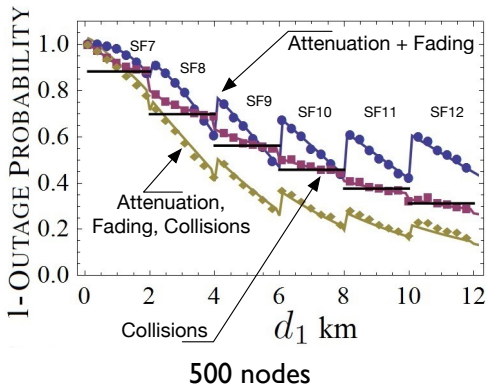
$$\begin{aligned} f_{X_i}(z) &= \int_{g(l_{j+1})}^{g(l_j)} \frac{1}{x} f_{g(d_i)}(x) f_{|h_i|^2}(z/x) dx \\ &= \frac{\lambda^2 z^{-\frac{\eta+2}{\eta}}}{8\eta\pi |\hat{\mathcal{V}}(d_1)|} \left[\Gamma\left(1 + \frac{2}{\eta}, \frac{z}{g(x)}\right) \right]_{x=l_{j+1}}^{x=l_j}, \end{aligned} \quad (9)$$

supported on $z \in \mathbb{R}^+$, where $\Gamma(\cdot, \cdot)$ is the upper incomplete gamma function. Integrating (9) we arrive at the cdf of X_i

$$F_{X_i}(z) = \frac{z^{\frac{2}{\eta}} \lambda^2}{16\pi |\hat{\mathcal{V}}(d_1)|} \left[\frac{(e^{\frac{-z}{g(x)}} - 1) z^{\frac{2}{\eta}}}{g(x)^{\frac{2}{\eta}}} - \Gamma\left(1 + \frac{2}{\eta}, \frac{z}{g(x)}\right) \right]_{x=l_{j+1}}^{x=l_j} \quad (10)$$

↑↑ Check out the cool math formulas! ↑↑

Previous work (cont.)



- HI — Outage due to attenuation
- QI (or QI) — Outage due to collision

Several follow-up papers... e.g. taking into account **inter-SF interference** (Mahmood *et al.*, 2018), **antenna diversity** (Hoeller *et al.*, 2018)...

The devil is in the details

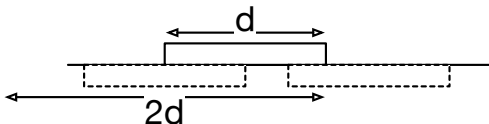
- **1% duty cycle for all nodes, regardless of SF**

This means that the application changes the amount of data depending of the SF!? — I don't think so

- Also, there are 3+ channels per band!
- **Collision probability:** given by “the expected number of concurrently transmitting end-devices”: $N_{\text{nodes}}(\text{SF}) \times 1\%$

But this is **Aloha!**

⇒ the probability of collision is $2 \times N_{\text{nodes}}(\text{SF}) \times 1\%$



- HI on the graph does not match the provided formula
No big deal – the formula does not really make sense anyway
(a mashup of free space and 2 ray ground)
- **Arbitrary** SF boundaries at 2, 4, 6, 8 and 12 km (really?)

So, can we tidy things up?

- There are at least 3 channels per band \Rightarrow duty cycle: **0.33%**
- Use **same traffic for all SF**:
 - ✓ Saturate SF12
 - ✓ 59B, 2.466 s of time on air, 1 packet / 747 s per frequency channel
 - ✓ We will be able to repeat this packet **6 times!**
(3 times in subband **h1.3**, 3 times in **h1.4**)
 - ✓ 6 repetitions \rightarrow **40% PDR** (Packet Delivery Ratio) gives **95% data extraction**
— with **12 repetitions**, we need only **22% PDR** —
- Okumara Hata propagation model
(less favorable than anything else)
- Collision probability: use an Aloha/Poisson traffic model **with capture**
(works just as well as the “theory of order statistics”)
(Sorry, math nerds...)
- **Which SF** should each node pick? — This is not a detail!
LoRaWAN single gateway capacity — 7

Aloha with capture in a Rayleigh channel

- Probability of no interference : $\exp(-2v)$
where v : frame arrival intensity \times frame duration
- Probability of single interference, 6dB lower:

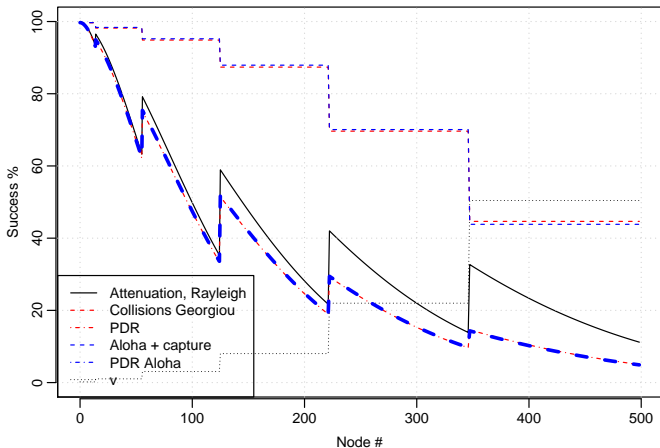
$$\frac{2}{5}v \exp((-2v))$$

(The probability that another frame is x times lower is $\frac{1}{x+1}$ with exp. distribution)

- With 2 or more interferers, we consider the frame lost (rare anyway)
- We consider that all nodes in a given SF get similar attenuation (mostly wrong for SF7, but there are no collisions, see below)

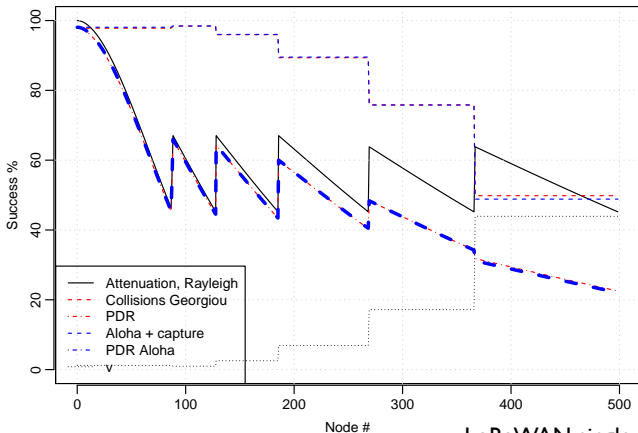
Regular SF boundaries

- SF boundaries at 2, 4, 6, 8 , 10 (and 12) km (more than half of the nodes use SF11 or SF12)
- 500 nodes, Antenna height 15 m, 6 dB gain



Hum —

- Clearly, this channel model does not give a range of 12km!
- Let's aim at a range giving empty channel PDR of e.g. **45% for SF12. (9.1 km)**
- Let's change of SF as soon as the SNR gives a PDR < 45%



500nodes

3.8 km

4.6 km

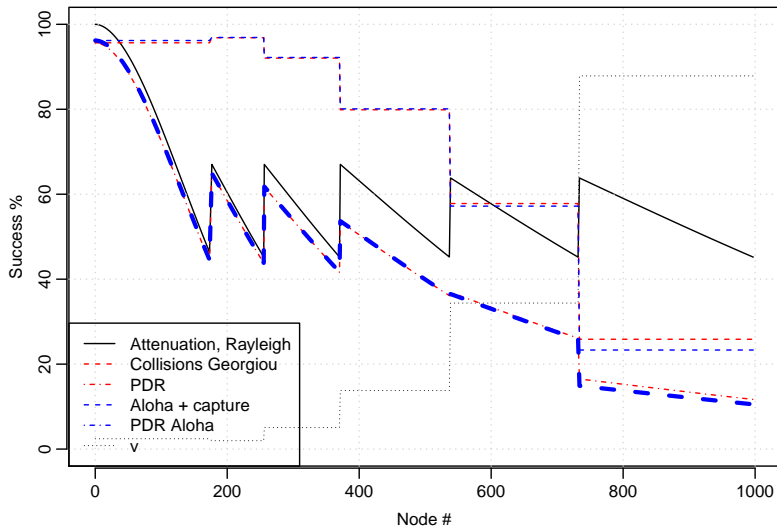
5.6 km

6.7 km

7.8 km

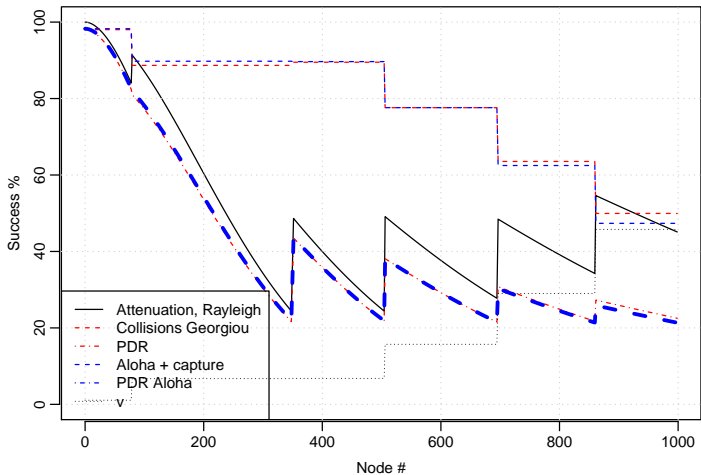
9.1 km

1000 nodes, PDR threshold = 45%



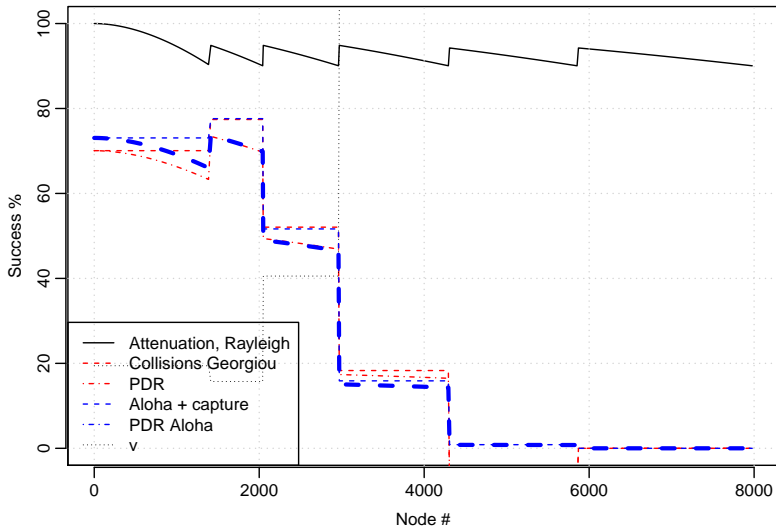
Adjusting SF boundaries 45%/1k nodes

- 5 thresholds to adjust
- Algorithm: Nelder Mead simplex: $\max(\min(\text{PDR}(\text{SF}))$

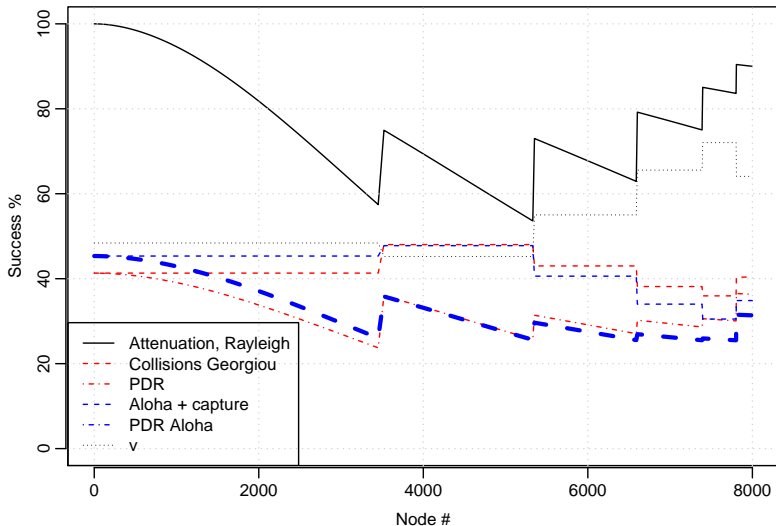


8000 nodes, PDR threshold = 90%

Range: 5.3 km



Adjusted boundaries, 90% PDR/8k nodes



Conclusion

- The smaller the radius, the more nodes can be handled
— up to 1000s of nodes!
→ And then, the downlink capacity will be the bottleneck
- The target SNR needs to be more and more discriminating for higher SF

Very true for short range and dense cells

- How do we control the nodes (Network server + ADR MAC messages)?
- Power control in SF7 zone would be much welcome!
(NB: increasing power then SF is also good in terms of power consumption, see M. N. Ochoa *et al.*, Evaluating LoRa Energy Efficiency for Adaptive Networks: From Star to Mesh Topologies, WiMob 2017)

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- What if multiple gateways?